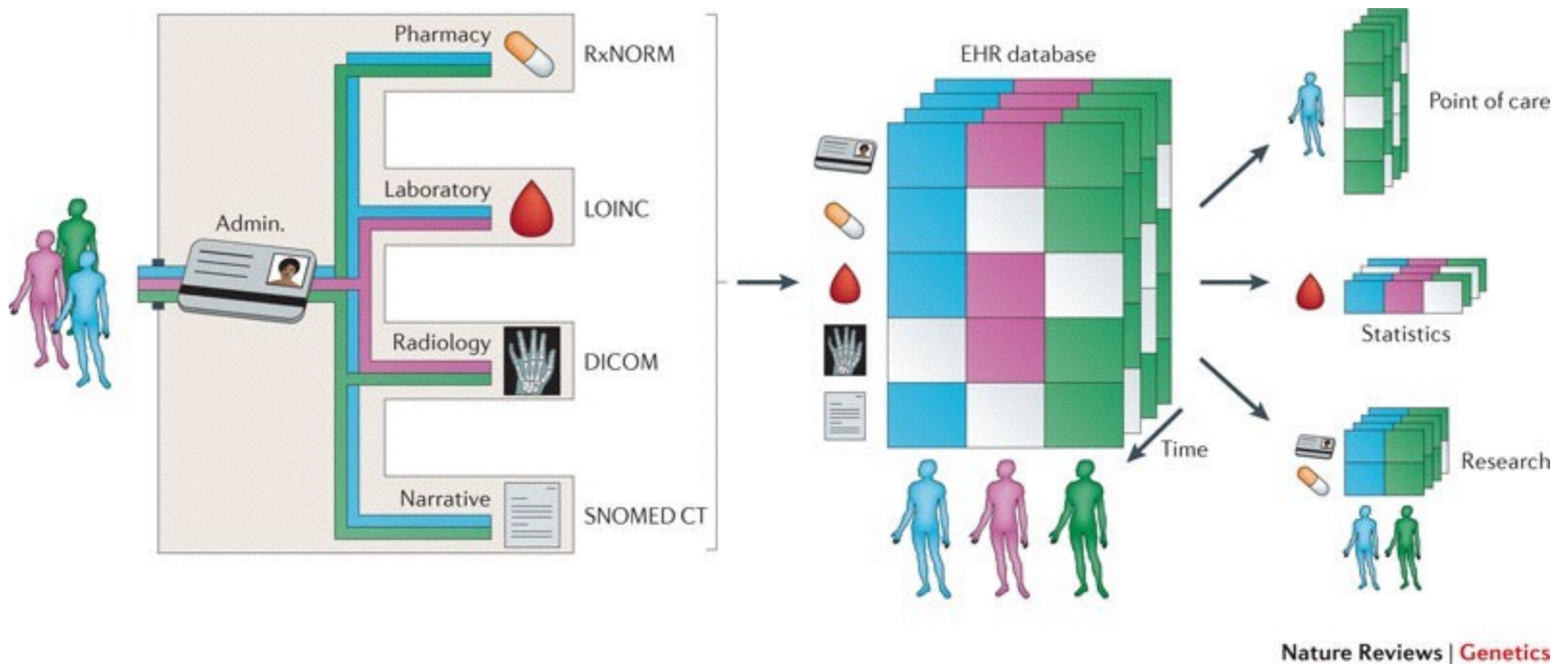


GRANITE: DIVERSIFIED, SPARSE TENSOR FACTORIZATION FOR ELECTRONIC HEALTH RECORD-BASED PHENOTYPING

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ELECTRONIC HEALTH RECORD (EHR)



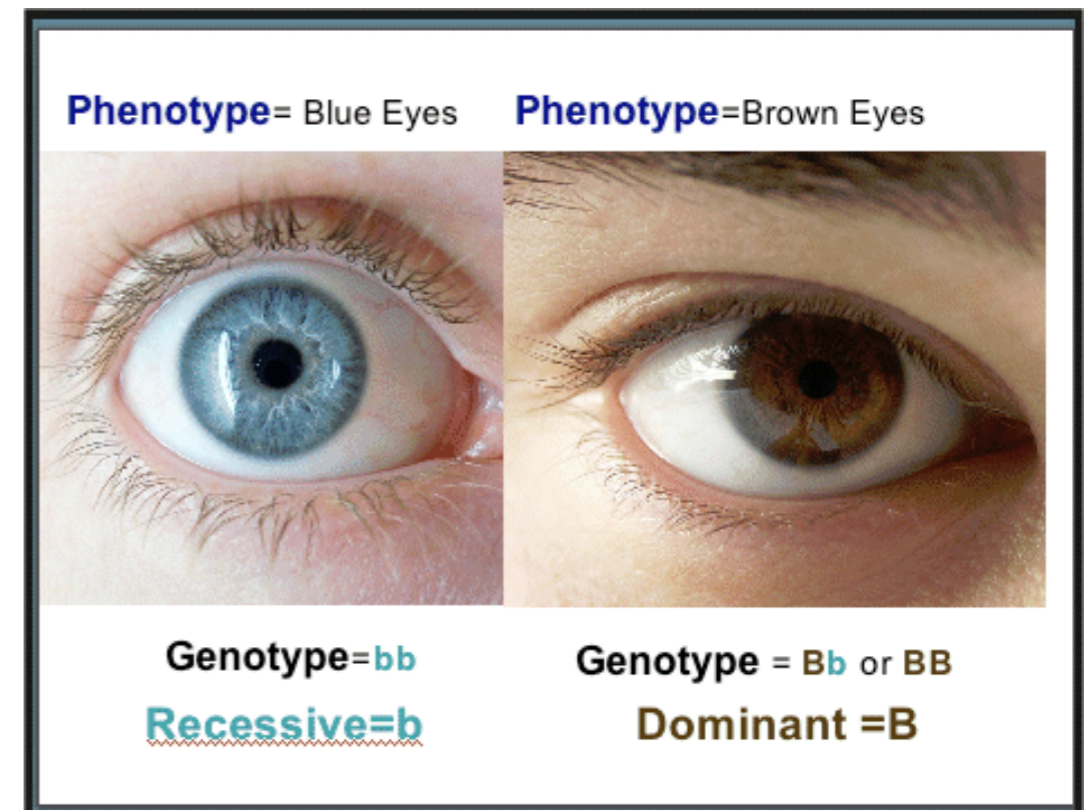
EHR: CHALLENGES

- ▶ Data
 - ▶ Diverse patient population
 - ▶ Heterogenous data types
 - ▶ Noisy & varying time scales
- ▶ Application
 - ▶ Good performance
 - ▶ Medical interpretability



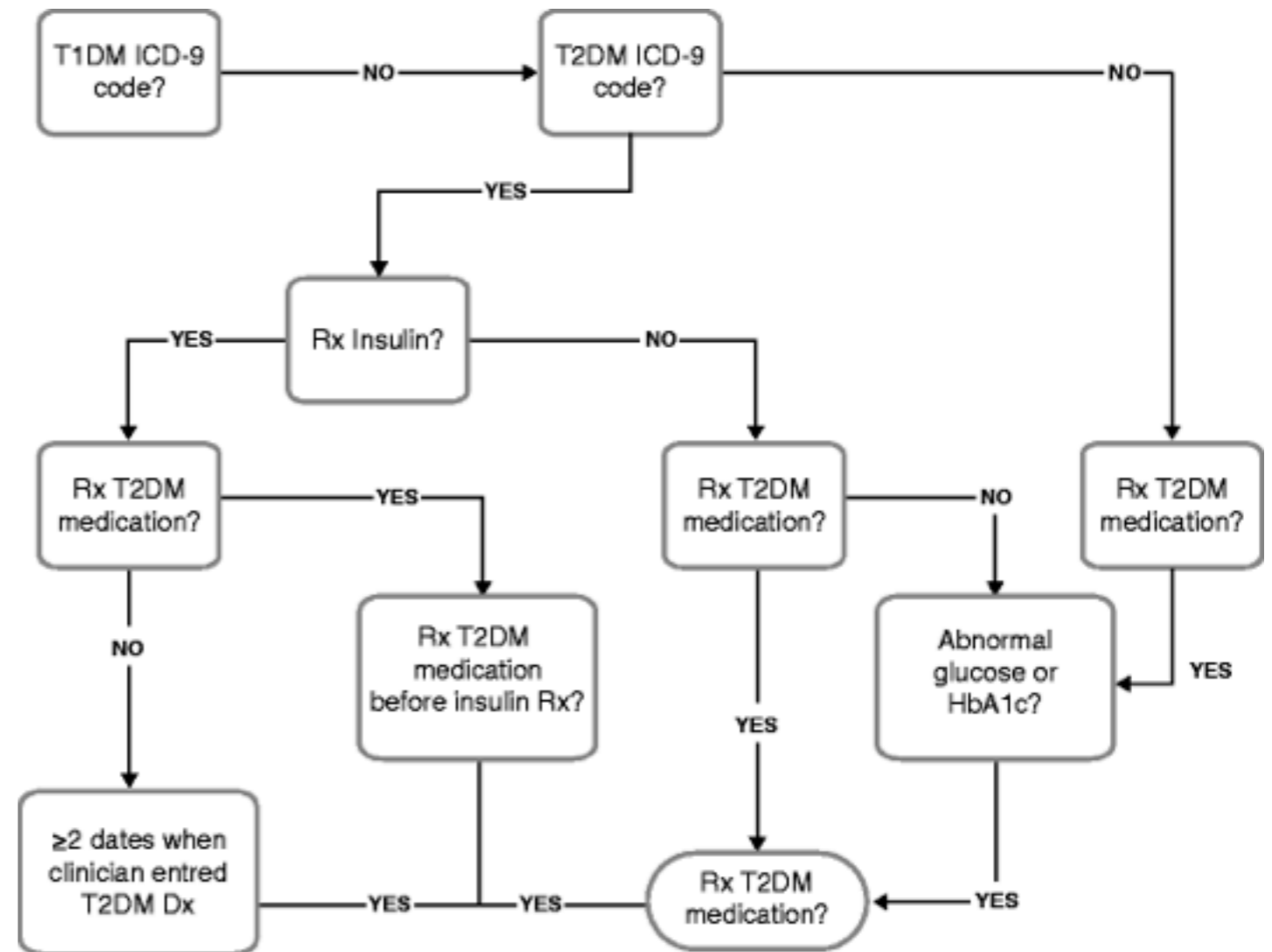
PHENOTYPE

- ▶ Observable characteristics of an organism determined by both genetic makeup and environmental influences
- ▶ Usage
 - ▶ Retrospective research
 - ▶ Clinical trial
 - ▶ Epidemiology/ population health

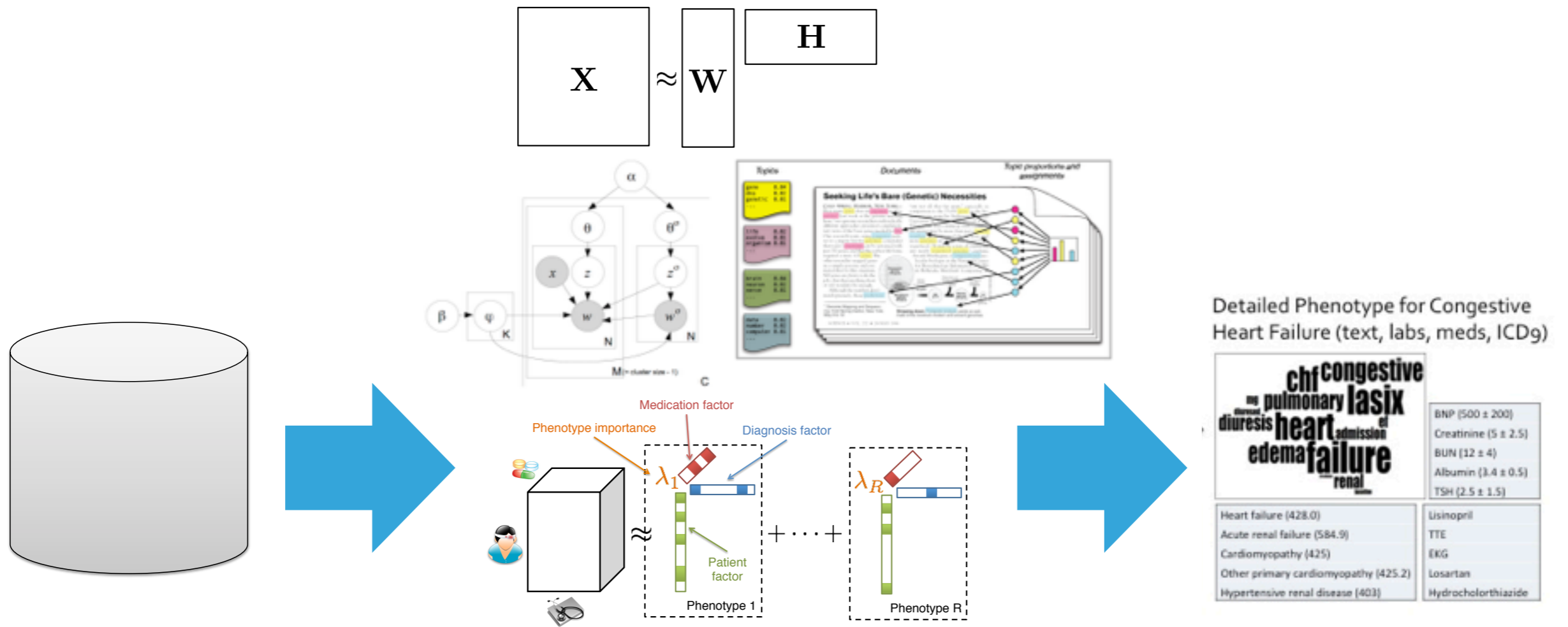


MODERN INTERPRETATION: EHR-BASED PHENOTYPING

- ▶ Specifications for identifying patients with a given condition of interest
- ▶ Concept representation easily understood (and therefore actionable) by clinicians



HIGH-THROUGHPUT PHENOTYPING: RECENT DEVELOPMENTS

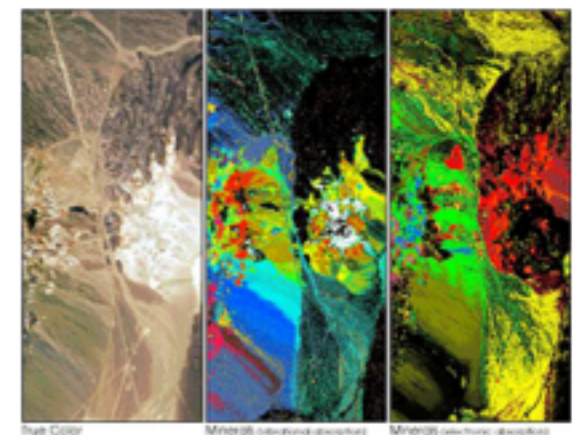
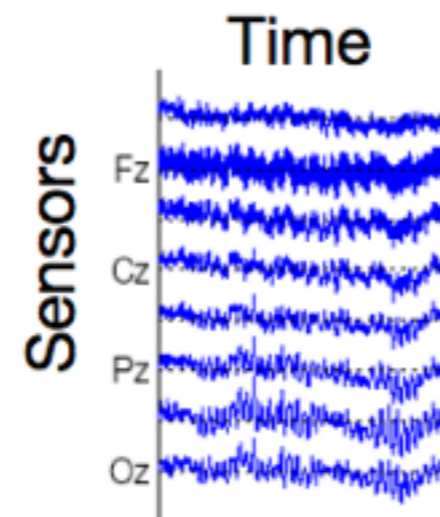
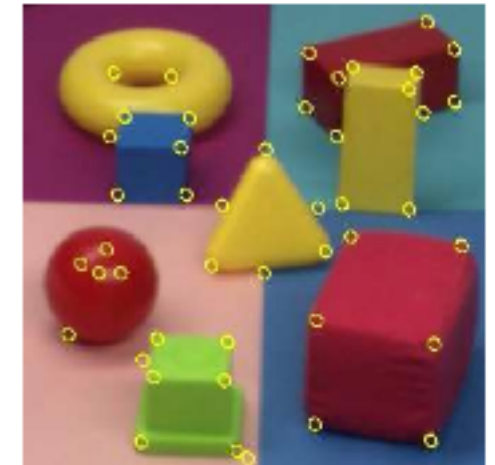
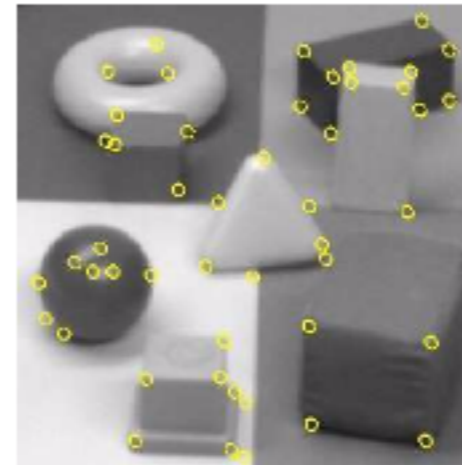


EHR database Machine learning algorithms Phenotypes

- ▶ These methods do not focus on generating sparse, diverse phenotypes with minimal supervision

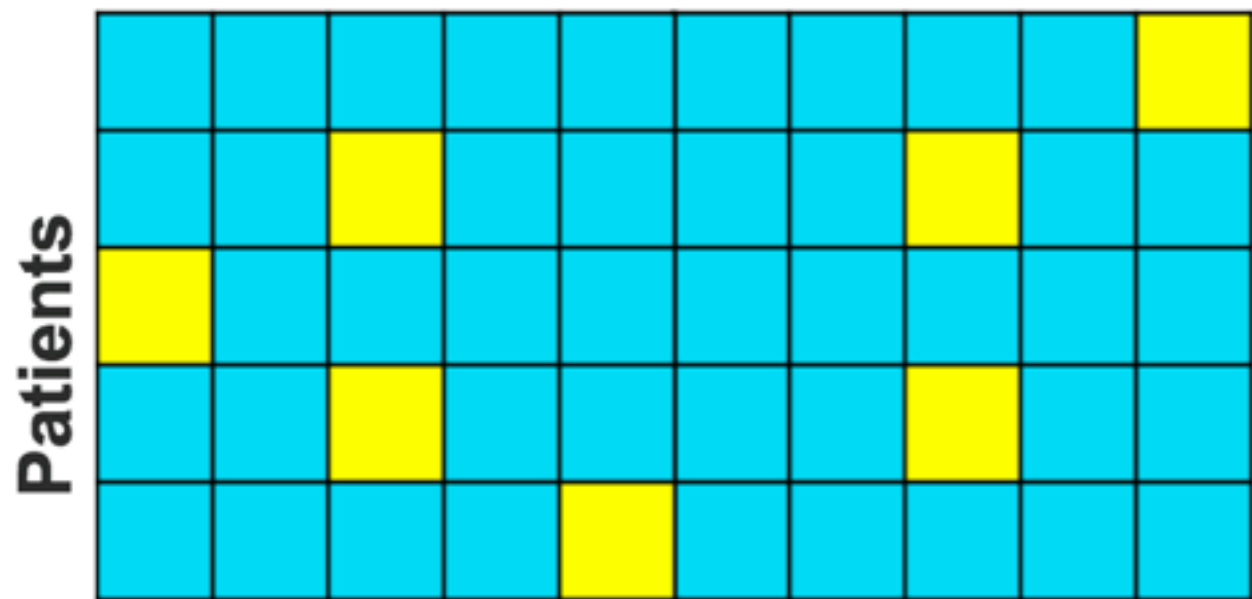
TENSORS (MULTIWAY ARRAYS)

- Generalization of matrices to multidimensional array
- Representation of an n-way interaction
- Captures hierarchical information in the structure
- Used in many domains



TENSORS

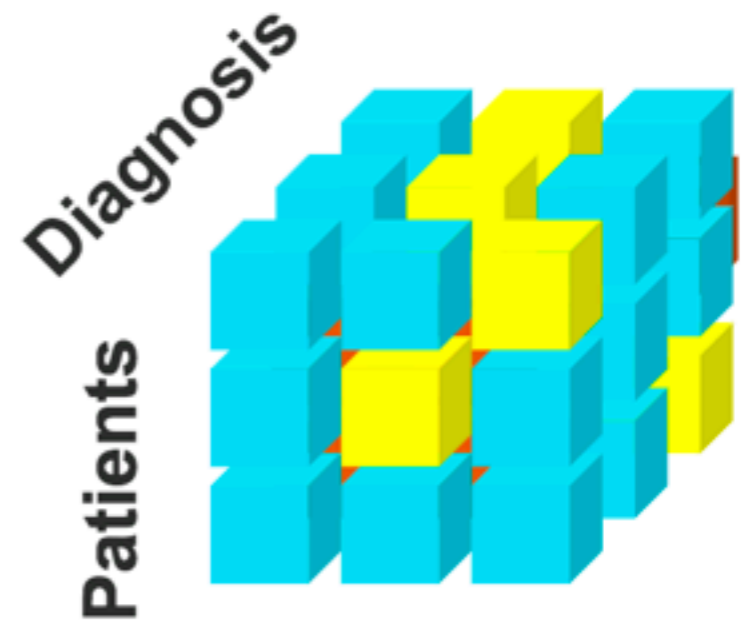
Diagnosis-Medication



Interaction matrix of medication for specific disease



Medication

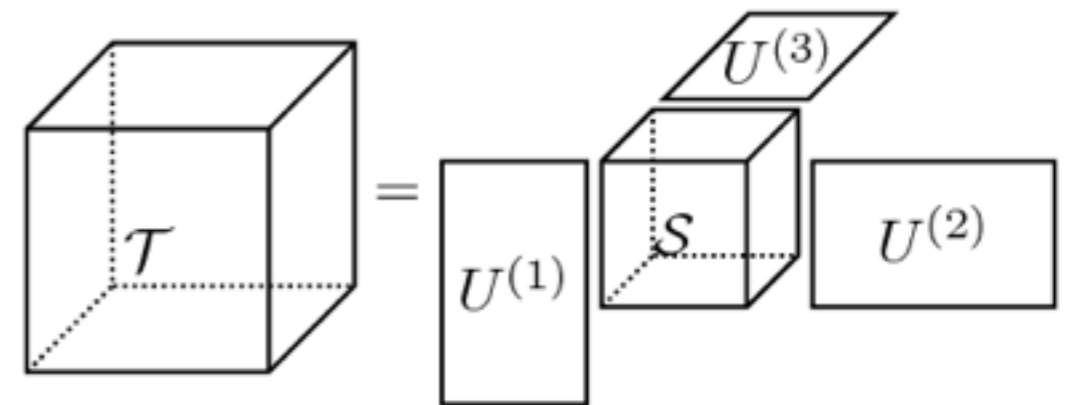
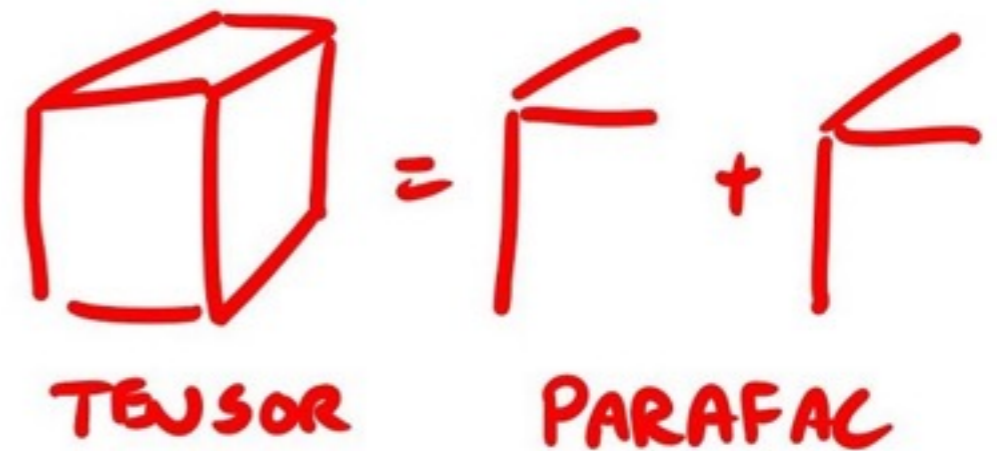


3-mode Feature Tensor

Each element represents # times a patient receives the medication to treat a specific diagnosis

TENSOR FACTORIZATION

- ▶ Generalization of matrix factorization
- ▶ Multiway structure information utilized during decomposition process
- ▶ Many decomposition models: CANDECOMP / PARAFAC (CP), Tucker, etc.



STANDARD CP ALTERNATING LEAST SQUARES (CP-ALS)

$$\begin{aligned} \min \quad & \sum_{\vec{i}} (x_{\vec{i}} - m_{\vec{i}})^2 \\ \text{s.t.} \quad & \mathcal{M} = \llbracket \boldsymbol{\lambda}; \mathbf{A}^{(1)}, \dots, \mathbf{A}^{(N)} \rrbracket \end{aligned}$$

- ▶ Objective function assumes Gaussian distribution for numeric data
- ▶ Can be altered to be nonnegative
- ▶ May not be suitable for count data

CP ALTERNATING POISSON REGRESSION (CP-APR)

- ▶ Poisson distribution for nonnegative, discrete data
- ▶ Nonnegative constraints
- ▶ Stochastic column constraints

$$\min f(\mathcal{M}) \equiv \sum_{\vec{i}} m_{\vec{i}} - x_{\vec{i}} \log m_{\vec{i}}$$

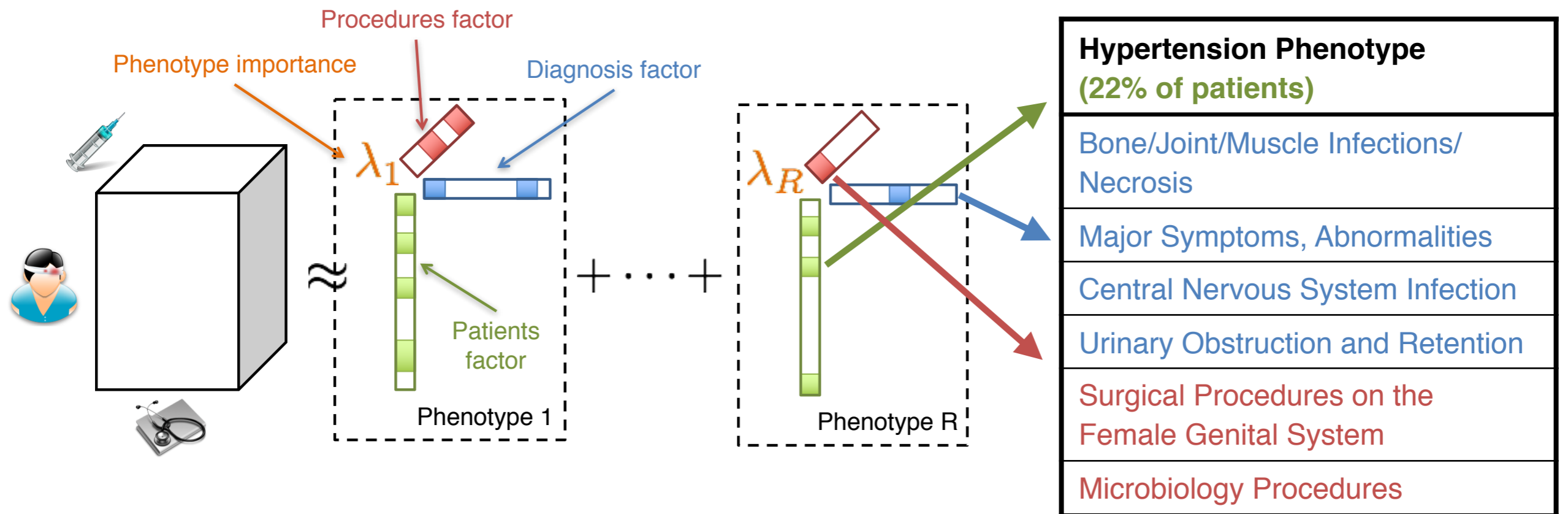
$$\text{s.t } \mathcal{M} = [[\boldsymbol{\lambda}; \mathbf{A}^{(1)}; \dots; \mathbf{A}^{(N)}]] \in \Omega$$

$$\Omega = \Omega_{\lambda} \times \Omega_1 \times \dots \times \Omega_N$$

$$\Omega_{\lambda} = [0, +\infty)^R$$

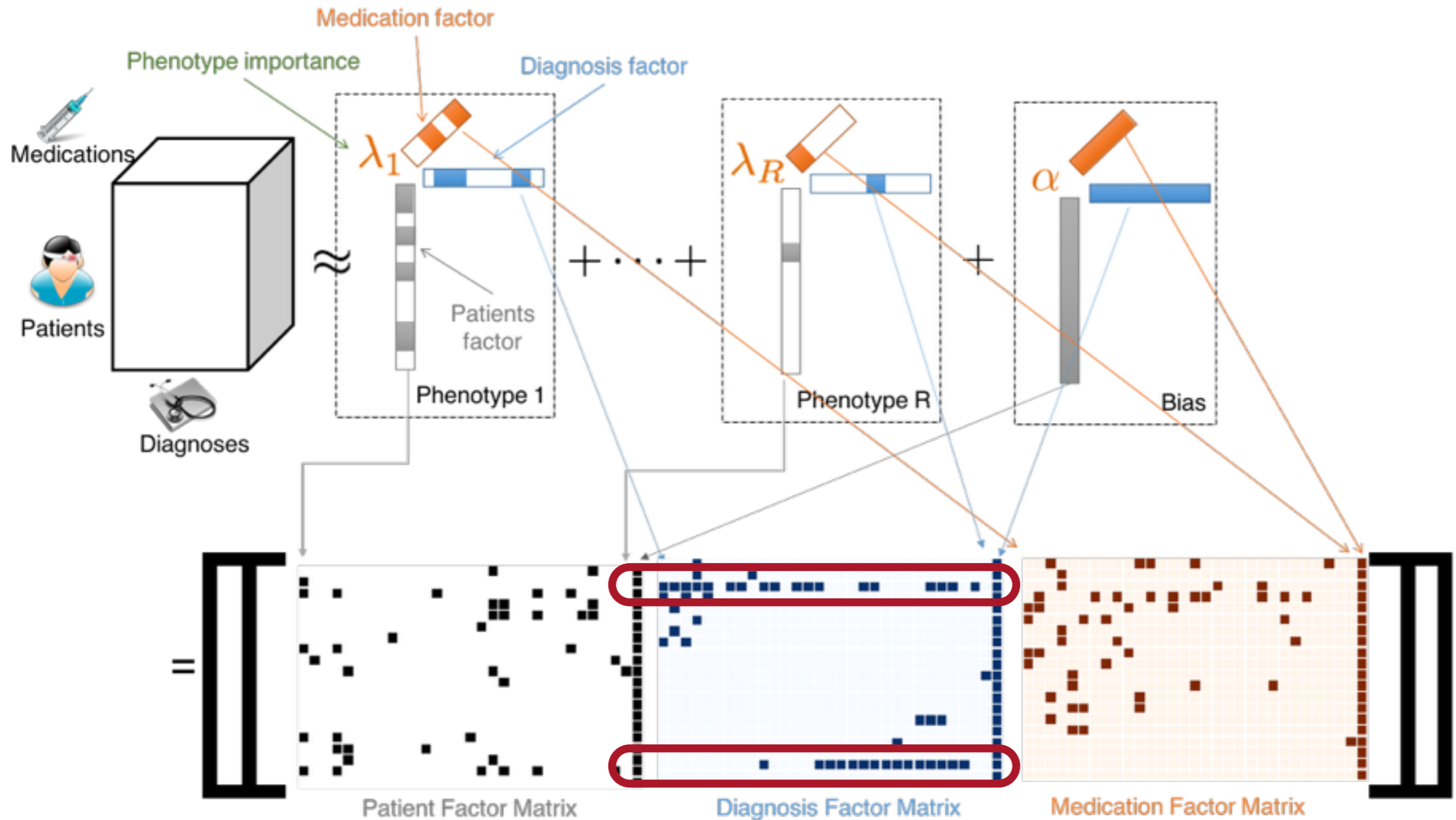
$$\Omega_n = \{\mathbf{A} \in [0, 1]^{I_n \times R} \mid \|\mathbf{a}_r\|_1 = 1 \ \forall r\}$$

LIMESTONE: PHENOTYPING VIA TENSOR FACTORIZATION



Nonzero elements are clinical characteristics with the conditional probability given the phenotype and mode

MARBLE: MOTIVATION FOR DIVERSE PHENOTYPES



OVERLAPPING ELEMENTS CAN BE DIFFICULT TO INTERPRET

GRANITE: DIVERSIFIED, SPARSE TENSOR FACTORIZATION

- ▶ Poisson model for count data
- ▶ Angular and ridge terms to reduce overlapping factors
- ▶ Simplex projection for better sparsity control
- ▶ Projected gradient descent to fit decomposition

**PUSH ELEMENTS
TO BE SMALL**

$$\min \left(\sum_{\vec{i}} (z_{\vec{i}} - x_{\vec{i}} \log z_{\vec{i}}) + \frac{\beta_1}{2} \sum_{n=1}^N \sum_{r=1}^R \sum_{p=1}^r \left(\max\left\{0, \frac{(\mathbf{a}_p^{(n)})^\top \mathbf{a}_r^{(n)}}{\|\mathbf{a}_p^{(n)}\|_2 \|\mathbf{a}_r^{(n)}\|_2} - \theta_n\right\} \right)^2 + \frac{\beta_2}{2} \sum_{n=1}^N \sum_{r=1}^R \|\mathbf{a}_r^{(n)}\|_2^2 \right)$$

$$\text{s.t. } \mathbf{Z} = [\sigma; \mathbf{u}^{(1)}; \dots; \mathbf{u}^{(N)}] + [\lambda; \mathbf{A}^{(1)}; \dots; \mathbf{A}^{(N)}]$$

$$\sigma > 0, \lambda_r \geq 0, \forall r$$

$$\mathbf{A}^{(n)} \in [0, 1]^{I_n \times R}, \mathbf{u}^{(n)} \in (0, 1]^{I_n \times 1}, \forall n$$

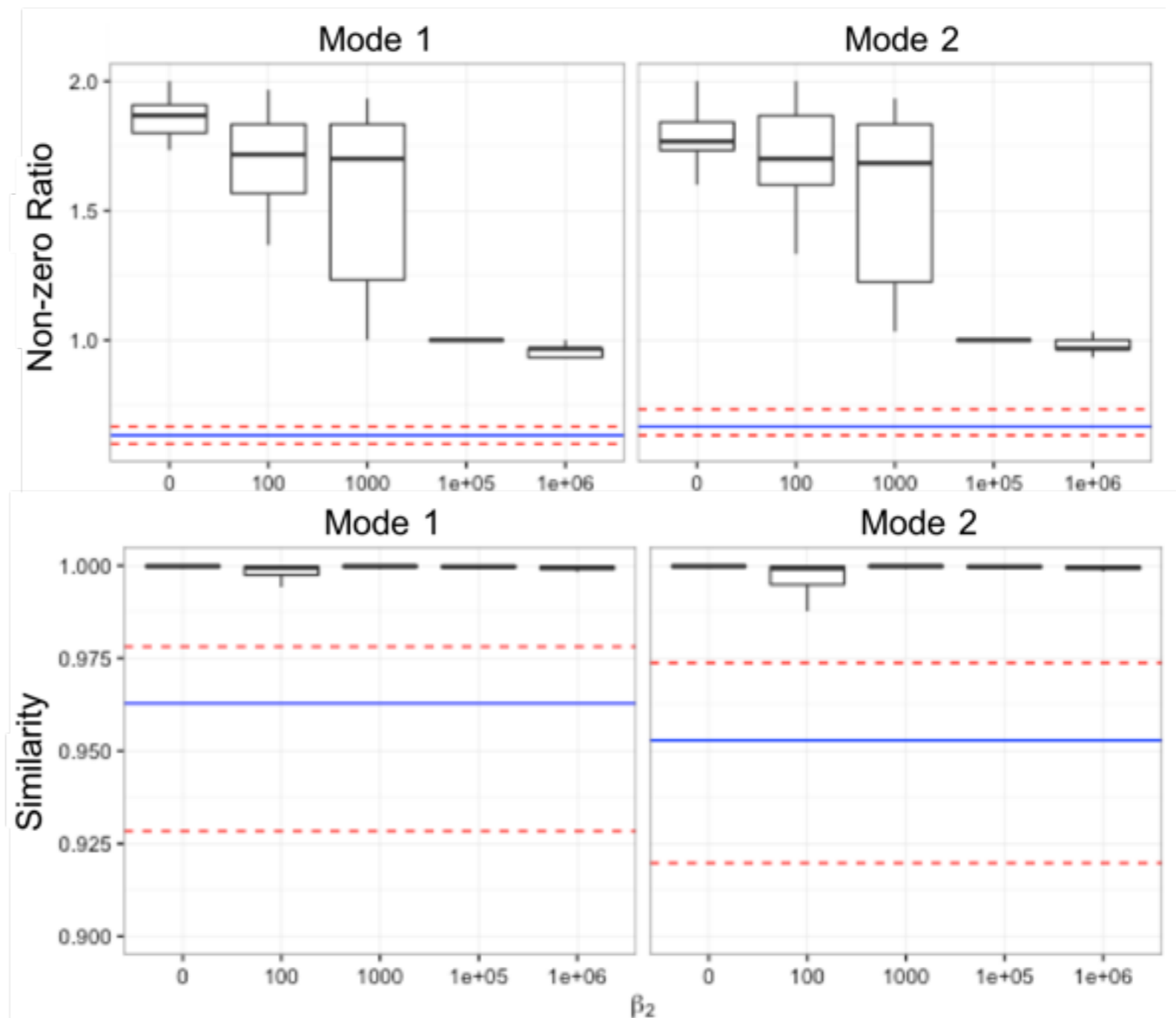
$$\|\mathbf{a}_r^{(n)}\|_1 = \|\mathbf{u}^{(n)}\|_1 = 1 \quad \forall n$$

**REDUCE COSINE
SIMILARITY FOR INTRA-
PHENOTYPE DIVERSITY**

SPARSITY CONTROL

SIMULATED TENSORS: ACCURATE RECOVERY

- ▶ Simulated 50 third-order tensor of size $40 \times 20 \times 20$ with rank of 5 with cosine similarity threshold set to .3
- ▶ Fit Granite and Marble decompositions



DATA: VANDERBILT UNIVERSITY SYNTHETIC DERIVATIVE

- ▶ Inpatient and outpatient billing and medication codes for nearly 2 million patients
- ▶ Focus on resistant hypertension
 - ▶ 1394 patients (33% cases) - manually identified by domain experts
 - ▶ 177 diagnoses (HCC categories)
 - ▶ 149 medications (MeSH PA)
- ▶ Compare Granite, Marble, CP-APR, CP-ALS, NMF

RESULTS

RESULTS: TOP 5 RESULTING PHENOTYPES

Granite

Phenotype 1
(15.43% of Patients)
Legally Blind
Major Symptoms, Abnormalities (1,2)
Polyneuropathy
Cerebrovascular Disease Late Effects, Unspecified
Multiple Sclerosis
anticonvulsants
bronchodilators
anxiolytics, sedatives, and hypnotics

Phenotype 2
(10.76% of Patients)
Specified Heart Arrhythmias
Major Symptoms, Abnormalities (1,2)
Heart Infection/Inflammation, Except Rheumatic
diuretics
beta-adrenergic blocking agents
antihyperlipidemic agents (2,5)

Phenotype 3
(5.92% of Patients)
Other Endocrine/Metabolic/Nutritional Disorders (3,5)
Severe Hematological Disorders
vitamins

Phenotype 4
(3.41% of Patients)
Rheumatoid Arthritis and Inflammatory Connective Tissue Disease
antirheumatics

Phenotype 5
(7.71% of Patients)
Other Endocrine/Metabolic/Nutritional Disorders (3,5)
antihyperlipidemic agents (2,5)

Marble

Phenotype 1
(13.27% of Patients)
Other Infectious Diseases (1,2,5)
Bone/Joint/Muscle Infections/Necrosis (ii)
Major Symptoms, Abnormalities (1,2,3,4,5)
antiemetic/antivertigo agents (1,2)
anticonvulsants
anxiolytics, sedatives, and hypnotics
antihistamines (1,2)

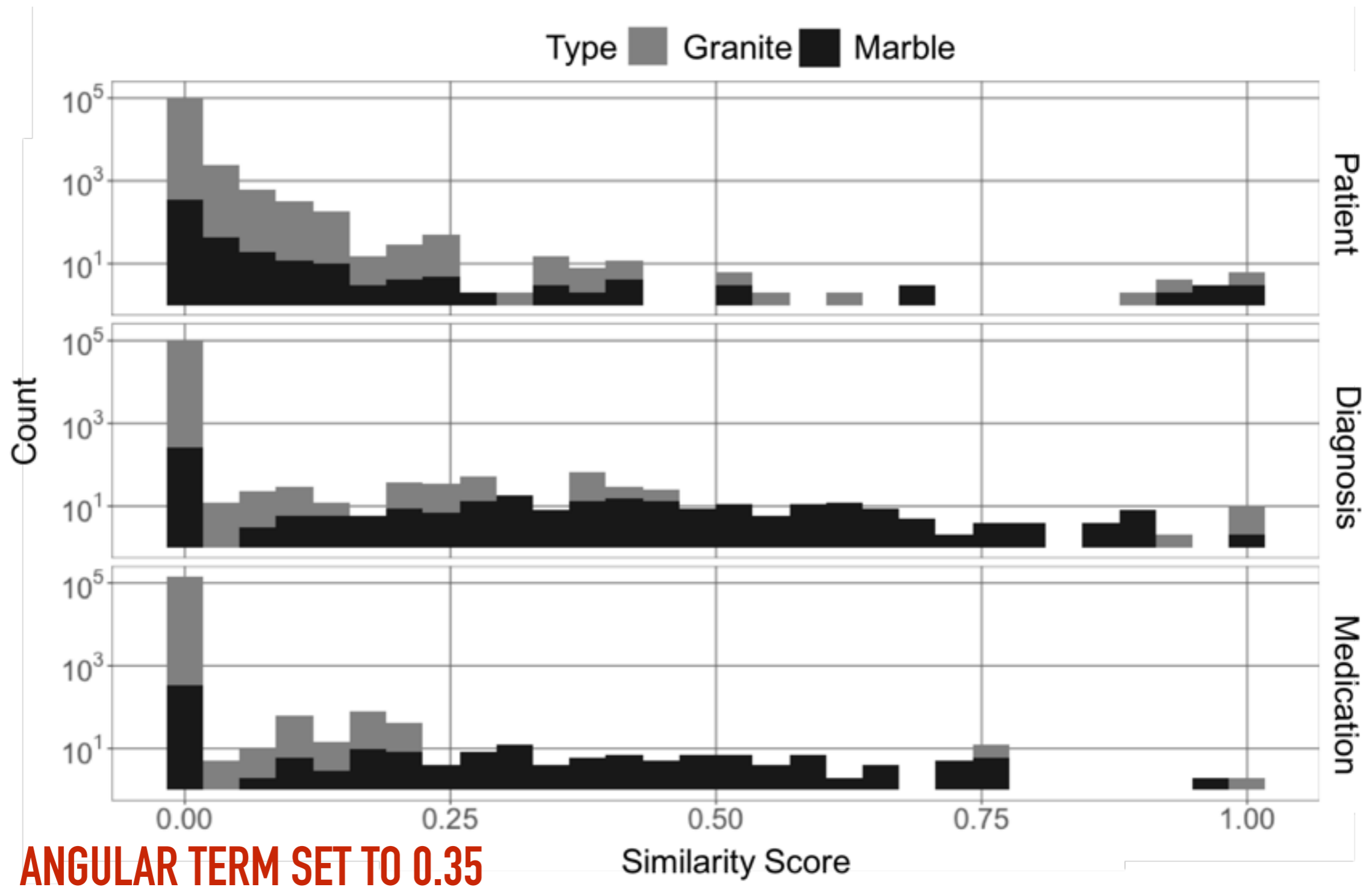
Phenotype 2
(9.6% of Patients)
Severe Hematological Disorders
Major Symptoms, Abnormalities (1,2,3,4,5)
Parkinson's and Huntington's Diseases
analgesics
antiemetic/antivertigo agents (1,2)
antihistamines (1,2)

Phenotype 3
(5.38% of Patients)
Other Infectious Diseases (1,2,5)
Bone/Joint/Muscle Infections/Necrosis (ii)
Major Symptoms, Abnormalities (1,2,3,4,5)
antifungals
antituberculosis agents
dermatological agents

Phenotype 4
(15.43% of Patients)
Major Symptoms, Abnormalities (1,2,3,4,5)
Coronary Atherosclerosis/Other Chronic Ischemic Heart Disease
Congestive Heart Failure
Hypertension
beta-adrenergic blocking agents
diuretics
antiarrhythmic agents
antihyperlipidemic agents

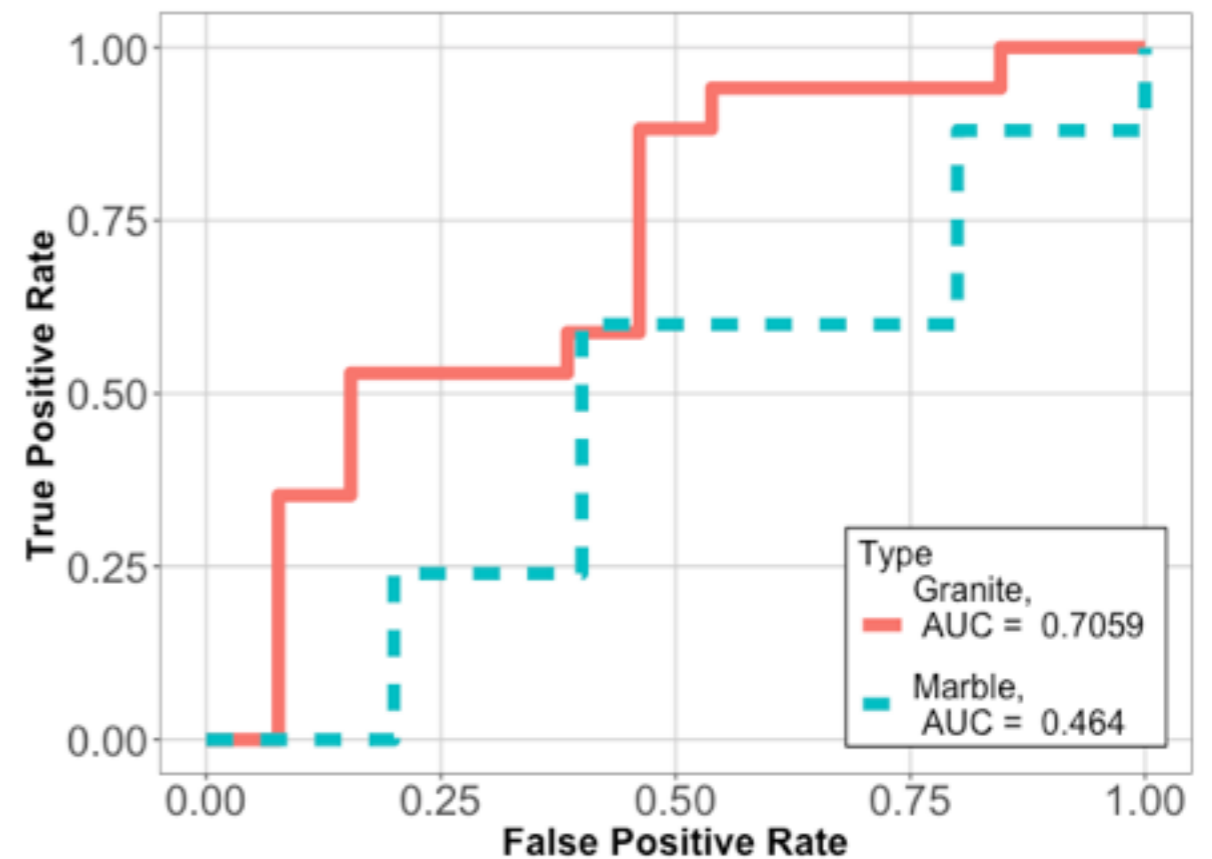
Phenotype 5
(5.38% of Patients)
Major Symptoms, Abnormalities (1,2,3,4,5)
Other Infectious Diseases (1,2,5)
laxatives
antacids
mouth and throat products
antiseptic and germicides

RESULTS: COSINE SIMILARITY



RESULTS: IMPORTANCE OF PHENOTYPE WEIGHTS

- ▶ Domain expert annotated phenotypes into 3 categories
 - ▶ Clinically relevant
 - ▶ Possibly clinically relevant
 - ▶ Not relevant
- ▶ Granite generated fewer clinically relevant ones than Marble



HIGH CORRELATION BETWEEN WEIGHTS AND CLINICAL RELEVANCY

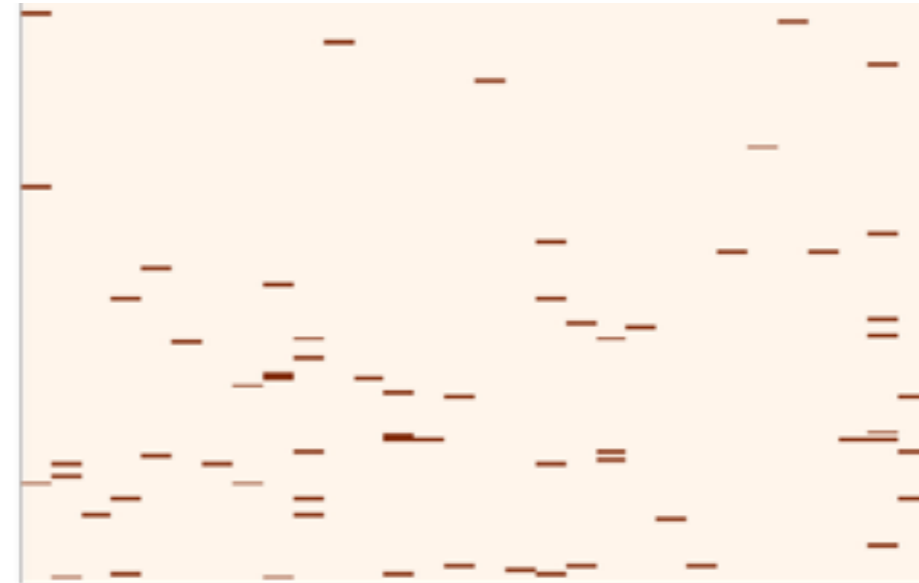
RESULTS: RESISTANT HYPERTENSION PREDICTION

- ▶ Task: Predict case vs controls
- ▶ 5 80-20 train/test splits with stratified sampling
- ▶ Logistic regression with Lasso
 - ▶ 10-fold CV to learn weight
 - ▶ Train on loadings (patient) matrix with $R = 30$

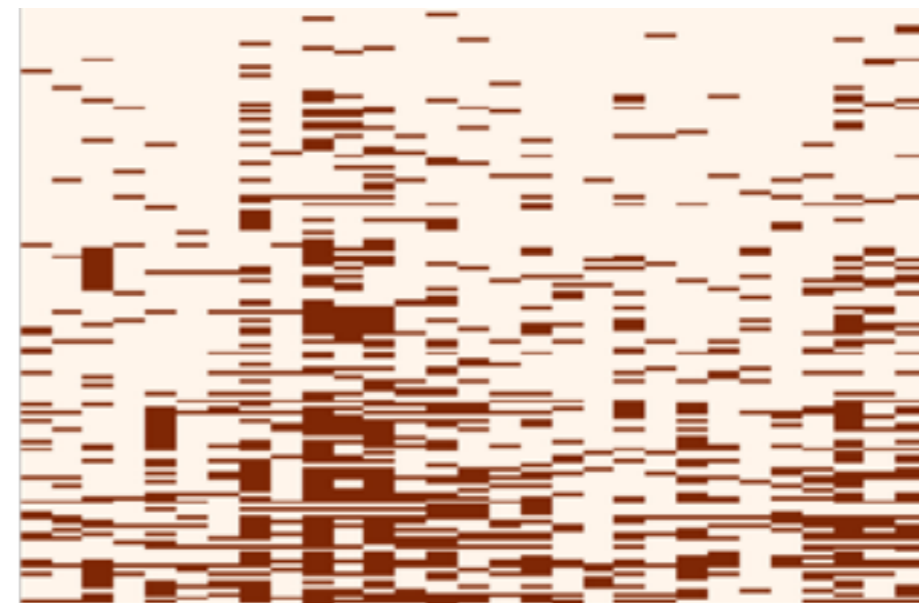
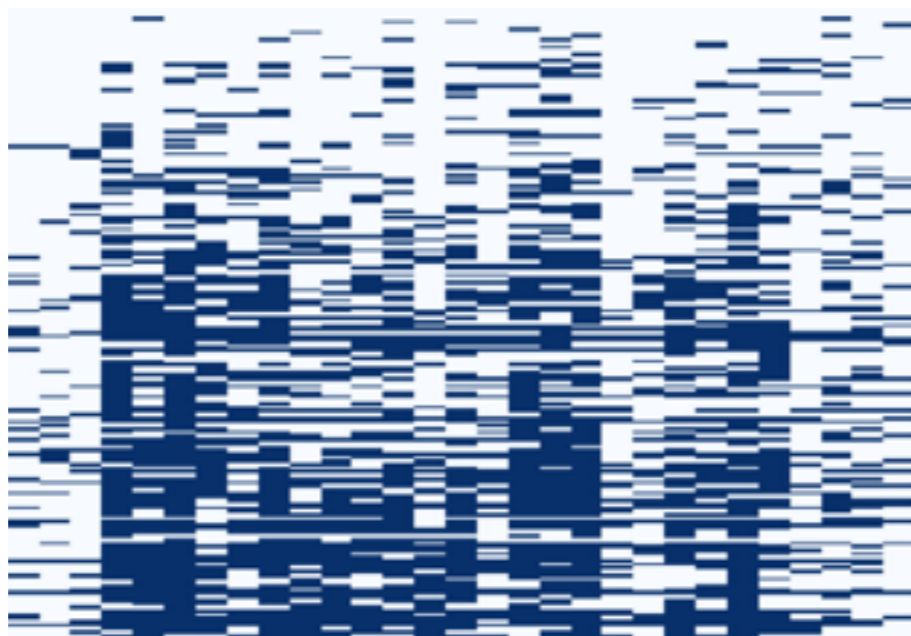
Model	AUC	NNZ / Phenotype
Granite	0.7298	4.63
Marble	0.7197	5.3330
CP-APR	0.7406	111.0000
CP-ALS	0.6765	113.1522
NMF	0.7203	N/A

RESULTS: NON-ZERO ELEMENTS

Granite



CP-APR



CONCLUSION

- ▶ Granite provides an unsupervised framework to extract concise and diverse phenotypes that retain predictive power

FUTURE WORK

- ▶ Provide weak supervision using outside data sources to increase the number of clinically relevant phenotypes

COLLABORATORS

- ▶ Emory University: Joyce C. Ho
- ▶ UT-Austin: Joydeep Ghosh
- ▶ GaTech: Jimeng Sun
- ▶ Vanderbilt: Joshua Denny & Bradley A Malin
- ▶ Northwestern: Abel N Kho



EMORY
UNIVERSITY



VANDERBILT
UNIVERSITY



Northwestern
University



Northeastern

Epic

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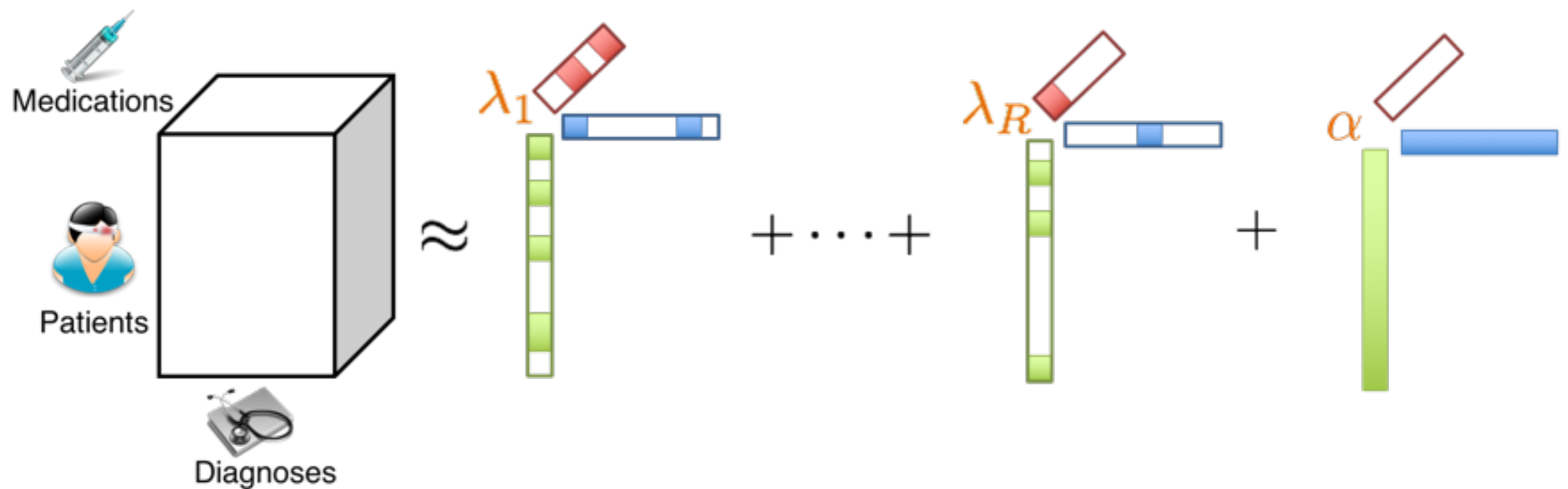


TEXAS

The University of Texas at Austin

FEATURE MATRIX

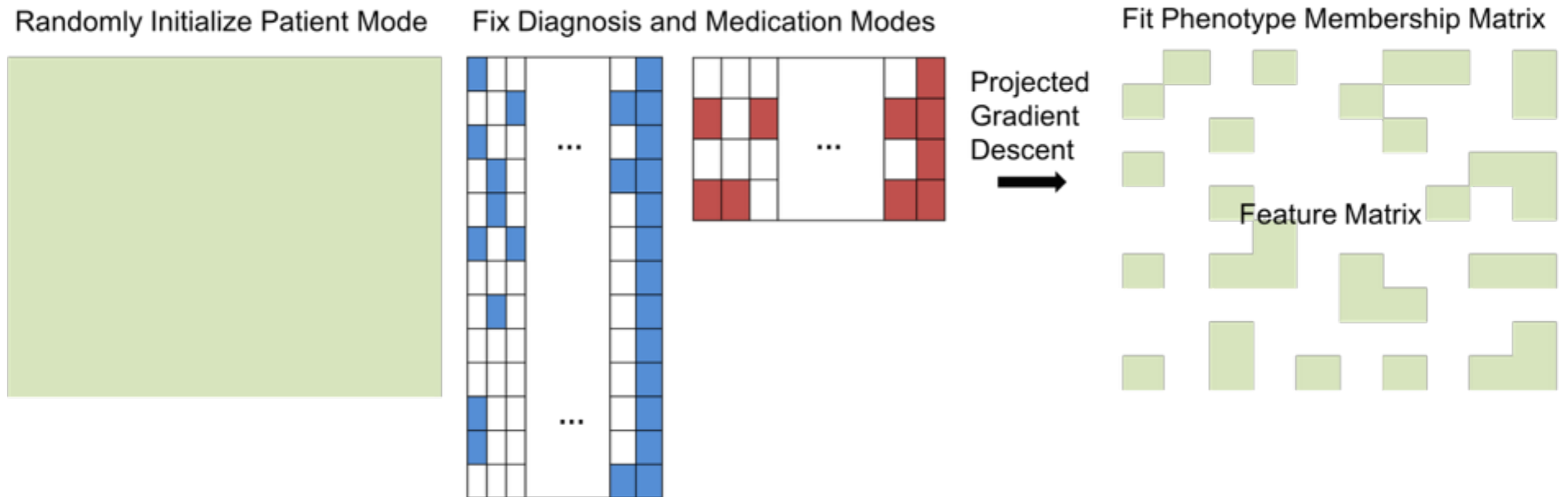
- ▶ Fit a decomposition on a set of patients X



- ▶ For a new set of patients X_{test} , fix diagnosis and medication modes and use projected gradient descent to fit a new patient mode
- ▶ Row normalize new patient mode to find a patient's membership to phenotypes

FEATURE MATRIX

- Fit a decomposition on a set of patients X_{train}



- For a new set of patients X_{test} , fix diagnosis and medication modes and use projected gradient descent to fit a new patient mode
- Row normalize new patient mode to find a patient's membership to phenotypes